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9.  $\sqrt{x^6}$

10.  $\sqrt{w^{10}}$

11.  $\sqrt{x^{16}}$

12.  $\sqrt{16a^2b^8}$

13.  $\sqrt{9x^{12}}$

*Tip: When taking roots of exponential expressions, keep the base and take half of the exponent.*

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*Tip: To check your answer, multiply the outer number twice and then multiply by the inner number to get what you started with.  $4 \cdot 4 \cdot 5 = 240$*

**Sample Problem 3: Simplify**  $\sqrt{x^{13}}$

**Solution:**  $\sqrt{x^{13}} = \sqrt{x^{12} \cdot x} = \sqrt{x^{12}} \cdot \sqrt{x} = x^6 \sqrt{x}$

**Student Practice: Simplify each radical expression.**

1.  $\sqrt{18}$  | 2.  $\sqrt{50}$

3.  $\sqrt{27}$  | 4.  $\sqrt{24}$

5.  $\sqrt{32}$  | 6.  $\sqrt{72}$

28.  $\sqrt{21}$  | 8.  $\sqrt{64}$

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$$9. \sqrt{w^8}$$

$$10. \sqrt{x^9}$$

$$11. \sqrt{a^{15}}$$

$$12. \sqrt{a^3}$$

$$13. \sqrt{a^5 b^{10}}$$

$$14. \sqrt{20x^7}$$





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5.  $2\sqrt{10} - 7\sqrt{40}$

6.  $5\sqrt{18} - 2\sqrt{50} + 6\sqrt{2}$

7.  $5\sqrt{2x^2} - 2\sqrt{200}$

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## 15.4 Multiplying and Dividing Radical Expressions

When multiplying two radical expressions, recall the product rule from before which states that the product of two radical expressions is the radical of the product.

### PRODUCT RULE

$$\sqrt{a} \cdot \sqrt{b} = \sqrt{a \cdot b}$$

**Sample Problem:** Multiply, then simplify  $\sqrt{12x^3y} \cdot \sqrt{6x^5y^4}$

**Solution:**

$$\sqrt{12x^3y} \cdot \sqrt{6x^5y^4} = \sqrt{12x^3y \cdot 6x^5y^4} = \sqrt{72x^8y^5} = \sqrt{36 \cdot 2 \cdot x^8 \cdot y^4 \cdot y} = 6x^4y^2\sqrt{2y}$$

**Student Practice:** Use the product rule to multiply, then simplify.

1.  $\sqrt{50} \cdot \sqrt{2}$  | 2.  $\sqrt{7} \cdot \sqrt{7}$

3.  $\sqrt{13} \cdot \sqrt{13}$  | 4.  $\sqrt{3} \cdot \sqrt{6}$

5.  $\sqrt{2x^3} \cdot \sqrt{8x^3y^4}$  | 6.  $\sqrt{x^3} \cdot \sqrt{x^2}$

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7.  $3\sqrt{5} \cdot 2\sqrt{10}$

To multiply radical expressions with more than one term, use the product rule discussed earlier along with the distributive property. Multiply the inside of the radicals together and the outside of the radicals together, **then simplify if possible**.

**Sample Problem:**     **Multiply**      $(2\sqrt{3} - 5\sqrt{2})(3\sqrt{3} + \sqrt{2})$

**Solution: (FOIL)**  $(2\sqrt{3} - 5\sqrt{2})(3\sqrt{3} + \sqrt{2}) = 2\sqrt{3} \cdot 3\sqrt{3} + 2\sqrt{3} \cdot \sqrt{2} - 5\sqrt{2} \cdot 3\sqrt{3} - 5\sqrt{2} \cdot \sqrt{2}$   
 $= 6\sqrt{9} + 2\sqrt{6} - 15\sqrt{6} - 5\sqrt{4}$   
 $= 6 \cdot 3 - 13\sqrt{6} - 5 \cdot 2$   
 $= 18 - 13\sqrt{6} - 10$   
 $= 8 - 13\sqrt{6}$

**Student Practice:**     **Multiply and simplify.**

1.  $\sqrt{3}(\sqrt{5} + \sqrt{2})$

2.  $(1 - \sqrt{7})(4 + 3\sqrt{7})$

3.  $(3\sqrt{2} - \sqrt{a})(3\sqrt{2} + \sqrt{a})$

4.  $(2\sqrt{5} - 3\sqrt{2})(\sqrt{5} + 4\sqrt{2})$

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5.  $(5 + \sqrt{x})^2$

6.  $(a - \sqrt{b})^2$

### **• Dividing Radical Expressions**

When dividing rational expressions, use the quotient rule mentioned before stating that the quotient of two radicals is the radical of the quotient.

#### **QUOTIENT RULE**

$$\frac{\sqrt{a}}{\sqrt{b}} = \sqrt{\frac{a}{b}}$$

*Sample Problem: Divide and simplify.*

$$\frac{\sqrt{24x^{11}}}{\sqrt{3x^7}}$$

*Solution:*  $\frac{\sqrt{24x^{11}}}{\sqrt{3x^7}} = \sqrt{\frac{24x^{11}}{3x^7}} = \sqrt{8x^4} = \sqrt{4 \cdot 2x^4} = 2x^2\sqrt{2}$

*Student Practice: Divide and simplify.*

7.  $\frac{\sqrt{75}}{\sqrt{3}}$

8.  $\frac{\sqrt{48y^9}}{\sqrt{3y^3}}$

$$9. \frac{\sqrt{24x^7}}{\sqrt{3x^2}}$$

$$10. \frac{\sqrt{18x^5}}{\sqrt{3x}}$$

### ● RATIONALIZING DENOMINATORS

Often times in mathematics it is useful to write a fraction without a radical in the denominator.

The process of writing a fraction with a radical in the denominator as an equivalent fraction without a radical in the denominator is called **rationalizing the denominator**. To **rationalize a denominator**, try the following:

- Multiply the numerator and denominator by a radical term that will make the bottom radicand a perfect square.

*Sample Problem:*     *Rationalize*      $\frac{3}{\sqrt{5}}$

*Solution:*      $\frac{3}{\sqrt{5}} \cdot \frac{\sqrt{5}}{\sqrt{5}} = \frac{3\sqrt{5}}{\sqrt{25}} = \frac{3\sqrt{5}}{5}$

*Student Practice: Rationalize each denominator.*

$$11. \frac{10}{\sqrt{3}}$$

$$12. \frac{\sqrt{3}}{\sqrt{7}}$$



13.  $\frac{\sqrt{5}}{\sqrt{x}}$



14.  $\frac{3}{\sqrt{8}}$

15.  $\frac{4}{3\sqrt{2}}$



16.  $\sqrt{\frac{2}{3}}$





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*Student Practice: Solve each equation for  $x$ .*

1.  $\sqrt{x} + 11 = 15$

| 2.  $\sqrt{10x-1} - 6 = 1$

3.  $\sqrt{9x+10} + 5 = 15$

| 4.  $\sqrt{5x+4} = \sqrt{x+8}$

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$$5. \sqrt{24+2x} = x$$

$$6. \sqrt{8x+32} - 4 = x$$

$$7. \sqrt{2x+1} + 6 = 3$$

